#  <br> Lower School Scholarship 2023 

## MATHEMATICS

1 hour

## Name:

School:
Date:

Equipment required: pen, pencil, ruler, eraser.
Instructions to Candidates:

- Attempt all questions. Do not worry if you don't manage to do them all.
- Calculators may not be used.
- Show ALL working.
- Check your answers for accuracy.
- Total marks for test : 100

1. A recipe for 8 servings of noodle pudding uses the following ingredients:

125 g butter
250 g noodles
4 eggs
125 g cottage cheese
80 g raisins
140g sugar
a) How much of each ingredient would be needed for a party of 32 people?
$\qquad$ butter
$\qquad$ noodles
$\qquad$ eggs
$\qquad$ cottage cheese
$\qquad$ raisins
$\qquad$ sugar
b) How much of each ingredient would be needed for a different party, of 4 people?
$\qquad$ butter
$\qquad$ noodles
$\qquad$ eggs
$\qquad$ cottage cheese
$\qquad$ raisins
$\qquad$ sugar
2. Write an algebraic expression for each of the following:
a) The number of pence in $m$ pounds
b) The cost of $n$ oranges and three times that number of lemons, when an orange costs 56 p and a lemon costs half as much.
$\qquad$ (3)
(Total for question is $\mathbf{4}$ marks)
3.


Patton 1
Pattern 2
Patter 3
a) Draw the $5^{\text {th }}$ pattern
b) How many matchsticks would be needed to make the $5^{\text {th }}$ pattern?
$\qquad$ (1)
c) Write down the number of squares in the nth pattern.
$\qquad$
d) Write down the number of matchsticks in the nth pattern.
4. a) Simplify: $3 a(2 a+3 b)-5\left(a^{2}-b\right)$
b) $c=3, d=-7, e=-4, f=0$

Find the value of
i) $c d^{2}-e$
$\qquad$ (3)
ii) $d e f+4 c e^{2}$
5. The area of a rectangle is $21 \frac{1}{4} \mathrm{~cm}^{2}$. The length is $7 \frac{1}{2} \mathrm{~cm}$. What is its width?
6. a) A car costs $£ 7000$ and decreases in value by $20 \%$ in the first year and $10 \%$ in each subsequent year.

What will the value of the car be after three years?
$\qquad$
b) Sipho travels 555 km . It takes him 7.5 hours.

What is his average speed?
7. Find the number which fulfils the following:

The sum of the number and 5 less than double the number is 34 .
8. Find the size of the angles in the diagram and state the angle fact you use in your calculation. The diagram is not drawn to scale.

$\qquad$
$a=$
$b=$
(2)
e =
$\mathrm{f}=$
9. Simplify:
a) $5 x y \times 7 x y z \times 2 z$
$\qquad$ (3)
b) $20 a^{2} b^{4} \div 10 a^{3} b^{5}$
10. a) What is the area of the shape (not drawn to scale)?

b) i) Find the total length of all the lines in the following diagram.

The diagram is not drawn to scale.

Ii) Find the area of the shaded part
11. In Beth's freezer there are

4 choc-ices,
8 lemon whirls
5 strawberry cream ices
7 toffee sundaes
Beth puts her hand into the freezer and takes the first iced dessert that she touches.
a) What is the probability that it is a fruity ice cream?
b) What is the probability that it is a coffee ice?

Beth replaces the ice she takes and she then takes and eats a toffee sundae. Her brother Ben chooses and eats a lemon whirl.

Her sister Jess then takes one at random.
c) What is the probability that it is a choc-ice?
d) What is the probability that it is not a strawberry cream?
12. Find the value of $j$
a) $7(j+3)+3 j+1=2(j-13)$
find the value of $k$
b) $\frac{3 k}{2}-4=k+1$
13.

a) Write down the equation of the straight line shown on the graph:
b) Draw a line which is perpendicular to the given line, passing through point $A$
c) Write down the equation of this new line
14. The frequency table below shows the number of sweets in each of a selection of bags of sweets.

| Number of sweets | Number of bags |
| :---: | :---: |
| 10 | 2 |
| 11 | 4 |
| 12 | 8 |
| 13 | 1 |

a) What is the modal (mode) number of sweets in a bag?
b) What is the median number in a bag?
$\qquad$ (2)
c) Calculate the mean number of sweets per bag
$\qquad$ (3)
d) What is the range of the number of sweets? $\qquad$
15. Find the values of $m$ and $n$ if

$$
\begin{aligned}
& 3 m-4 n=-26 \\
& 2 m+3 n=11
\end{aligned}
$$

$m=$ $\qquad$
$n=$ $\qquad$
(Total for question is $\mathbf{5}$ marks)

## END OF QUESTIONS

Check your work and, if you have time, try the following

1. In a Maths class there are 3 boys for every 2 girls.

The average age of the boys is 14 years 2 months.
The average age of the girls is 13 years 4 months
What is the average age of the class?
2. What is the ratio of the areas $A B C D$ : ACDF ?

3. A cold water tap fills a bath in $t$ minutes

A hot water tap fills the bath in half the time.
If they both run together they fill the bath in 5 minutes.
Find $t$

